M.C.M. (Semester—II) Examination OPERATION RESEARCH TECHNIQUES Paper—2 MCM 5

Time: Three Hours]

[Maximum Marks: 80

N.B.:— (1) Due credit will be given to neatness and adequate dimensions.

- (2) Assume suitable data wherever necessary.
- (3) Illustrate your answer with the help of neat sketches wherever necessary.
- (A) Explain limitation of Linear Programming.

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(B) Use the Graphical method to solve the following LP problem:

Maximize $Z = 2x_1 + 4x_2$

Subject to constraint

$$x_1 + 2x_2 \le 4$$

$$2\mathbf{x}_1 + \mathbf{x}_2 \le 6.$$

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(C) Explain application area of linear programming.

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OR

2. (A) Use the simplex method to solve the following LP problem:—

Max.
$$Z = 20x_1 + 6x_2 + 8x_3$$

subject to

$$8x_1 + 2x_2 + 3x_3 \le 250$$

$$4x_1 + 3x_2 \le 150$$

$$2x_1 + x_2 \le 50$$

and $x_1, x_2, x_3 \ge 0$.

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(B) Use the Big-M method to solve the following LP problem :—

Minimize $Z = 5x_1 + 3x_2$

Subject to constraints

$$2x_1 + 4x_2 \le 12$$

$$2x_1 + 2x_2 = 10$$

$$5x_1 + 2x_2 \ge 10$$

and $x_1, x_2 \ge 0$.

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- (A) Solve the following game. Find:
 - (1) Value of the game
 - Does the game have a saddle point?

Piayer B Player A

Tasks (B) II Ш IV 8 17 26 11 4 В 13 28 26 Subordinates 38 19 18 15 26 24 19 10

How should the tasks be allocated to subordinates so as to minimize the total Man-hours?

(C) Determine an initial basic solution to the following transportation problem by using VAM method:-

| | Dl | D2 | D3 | Supply |
|--------|----|----|----|--------|
| S1 | 7 | 3 | 4 | 2 |
| S2 | 2 | 1 | 3 | 3 |
| S3 | 3 | 4 | 6 | 5 |
| Demand | 4 | 1 | 5 | |

OR

- (A) Determine an initial basic feasible solution to the following transportation problem by 4. using:--
 - (1) NWCM (2) LCM

| | | | Destination | | | |
|--------|--------|-----|-------------|-----|-----|--------|
| | | D1 | D2 | D3 | D4 | Supply |
| | Α | 11 | 13 | 17 | 14 | 250 |
| Source | В | 16 | 18 | 14 | 10 | 300 |
| | C, | 21 | 24 | 13 | 10 | 400 |
| | Demand | 200 | 225 | 275 | 250 | |

Tasks

I Π IIIŊ 8 26 17 11 13 28 4 26 Subordinates 38 19 13 15 19 26 24 10

How should the tasks be allocated to subordinates so as to minimize the total man-hours?

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WPZ--2783

(B)

5. (A) Find the sequence that minimizes the total elapsed time and processing time in hours required to complete the following jobs:—

| Job | : | 1 | . 2 | 3 | 4 | 5 | 6 |
|-----------|---|---|-----|---|---|---|---|
| Machine A | ; | 4 | 8 | 3 | 6 | 7 | 5 |
| Machine B | : | 6 | 33 | 7 | 2 | 8 | 4 |

(B) Explain:-

- (1) Purchase Cost
- (2) Carrying Cost
- (3) Ordering Cost
- (4) Total Inventory Cost.

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OR

6. (A) Find the sequence that minimizes the total elapsed time required to complete the following tasks. Each job is processed in order ABC:—

| Job | : | 1 | 2 | 3 | 4 | 5 |
|-----------|---|---|---|---|---|---|
| Machine A | : | 5 | 7 | 6 | 9 | 5 |
| Machine B | : | 2 | 1 | 4 | 5 | 3 |
| Machine C | : | 3 | 7 | 5 | 6 | 7 |

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(B) The following table gives the machine times in hours for 9 jobs and two machines:

| Job | : | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|------------|---|---|---|---|---|---|---|---|---|----|
| Machine I | : | 2 | 5 | 4 | 9 | 6 | 8 | 7 | 5 | 4 |
| Machine II | : | 6 | 8 | 7 | 4 | 3 | 9 | 3 | 8 | 11 |

Find the elapse time and ideal time.

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7. (A) A project has following activities and other characteristics:--

| Activity | Time Estimates (weeks) | | | | | |
|----------|------------------------|-------------|-------------|--|--|--|
| | Optimistic | Most likely | Pessimistic | | | |
| 1-2 | 1 | 3 | 5 | | | |
| 2–3 | 1 | 4 | 7 | | | |
| 2-4 | 1 | 3 | 5 | | | |
| 2-5 | 5 | 8 | 11 | | | |
| 36 | 2 | 4 | 6 | | | |
| 36 46 | 5 | 6 | 7 | | | |
| 57 | 4 | 5 | 6 | | | |
| 6–7 | 1 | 3 | 5 | | | |

- (1) Draw the network diagram.
- (2) Identify critical path.
- (3) Find out ET & LT.
- (4) Find out variance and standard deviation.

3+1+2+4

- (B) Explain:-
 - (1) Events
 - (2) Activities
 - (3) Activity-on-Node
 - (4) Activity-on-Arrow.

OR

- 8. (A) Explain:—
 - (1) Optimistic time
 - (2) Pessimistic time
 - (3) Most likely time.

(B) The table consists of the following activities and their estimated times:

| Activity | Predecessor | Time (days) |
|----------|-------------|-------------|
| A | | 2 |
| В | | 1 |
| C | A | 3 |
| D | А, В | 2 |
| Е | C, D | 1 |
| F | B, D | 3 |
| G | E, F | |

- (1) Draw Network diagram.
- (2) Find critical path.
- (3) Calculate project completion time.
- (4) Calculate total float and free float for each activity.

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- 9. (A) Give in detail the steps in Revised simplex method.
 - (B) What are the advantages and disadvantages of simulation methods?

OR

- 10. (A) What is simulation? Give its types.
 - (B) Use dual simplex method to solve the following LP problem:

Maximize $Z = 2x_1 - x_3$

Subject to constraints

$$\mathbf{x}_1+\mathbf{x}_2-\mathbf{x}_3 \geq 5$$

$$x_1 - 2x_2 + 4x_3 \ge 8$$

and
$$x_1, x_2, x_3 \ge 0$$

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